

# Visibility Culling using Hierarchical Occlusion Maps

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**Abstract:** We present hierarchical occlusion maps (HOM) for visibility culling on complex models with high depth complexity. The culling algorithm uses an object space bounding volume hierarchy and a hierarchy of image space occlusion maps. Occlusion maps represent the aggregate of projections of the occluders onto the image plane. For each frame, the algorithm selects a small set of objects from the model as occluders and renders them to form an initial occlusion map, from which a hierarchy of occlusion maps is built. The occlusion maps are used to cull away a portion of the model not visible from the current viewpoint. The algorithm is applicable to all models and makes no assumptions about the size, shape, or type of occluders. It supports approximate culling in which small holes in or among occluders can be ignored. The algorithm has been implemented on current graphics systems and has been applied to large models composed of hundreds of thousands of polygons. In practice, it achieves significant speedup in interactive walkthroughs of models with high depth complexity.

**CR Categories and Subject Descriptors:** I.3.5 [Computer Graphics]: Computational Geometry and Object Modeling

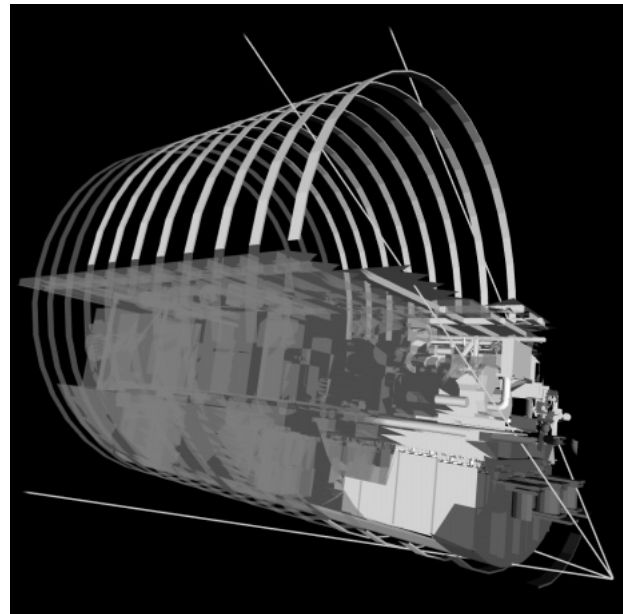
**Key Words and Phrases:** visibility culling, interactive display, image pyramid, occlusion culling, hierarchical data structures

## 1 Introduction

Interactive display and walkthrough of large geometric models currently pushes the limits of graphics technology. Environments composed of millions of primitives (e.g. polygons) are not uncommon in applications such as simulation-based design of large mechanical systems, architectural visualization, or walkthrough of outdoor scenes. Although throughput of graphics systems has increased considerably over the years, the size and complexity of these environments have been growing even faster. In order to display such models at interactive rates, the rendering algorithms need to use techniques based on visibility culling, levels-of-detail, texturing, etc. to limit the number of primitives rendered in each frame. In this paper, we focus on visibility culling algorithms, whose goal is to cull away large portions of the environment not visible from the current viewpoint.

Our criteria for an effective visibility culling algorithm are *generality*, *interactive performance*, and *significant culling*. Additionally, in order for it to be *practical*, it should be implementable on current graphics systems and work well on large real-world models.

**Main Contribution:** In this paper, we present a new algorithm for visibility culling in complex environments with high depth



**Figure 1:** Demonstration of our algorithm on the CAD model of a submarine's auxiliary machine room. The model has 632,252 polygons. The green lines outline the viewing frustum. Blue indicates objects selected as occluders, gray the objects not culled by our algorithm and transparent red the objects culled away. For this particular view, 82.7% of the model is culled.

complexity. At each frame, the algorithm carefully selects a small subset of the model as occluders and renders the occluders to build *hierarchical occlusion maps* (HOM). The hierarchy is an image pyramid and each map in the hierarchy is composed of pixels corresponding to rectangular blocks in the screen space. The pixel value records the *opacity* of the block. The algorithm decomposes the visibility test for an object into a two-dimensional overlap test, performed against the occlusion map hierarchy, and a conservative *Z* test to compare the depth. The overall approach combines an *object space* bounding volume hierarchy (also useful for view frustum culling) with the *image space* occlusion map hierarchy to cull away a portion of the model not visible from the current viewpoint. Some of the main features of the algorithm are:

1. **Generality:** The algorithm requires no special structures in the model and places *no restriction* on the types of occluders. The occluders may be polygonal objects, curved surfaces, or even not be geometrically defined (e.g. a billboard).
2. **Occluder Fusion:** A key characteristic of the algorithm is the ability to *combine* a “forest” of small or disjoint occluders, rather than using only large occluders. In most cases,

the union of a set of occluders can occlude much more than what each of them can occlude taken separately. This is very useful for large mechanical CAD and outdoor models.

3. **Significant Culling:** On high depth complexity models, the algorithm is able to cull away a significant fraction (up to 95%) of the model from most viewpoints.
4. **Portability:** The algorithm can be implemented on most current graphics systems. Its main requirement is the ability to read back the frame-buffer. The construction of hierarchical occlusion maps can be accelerated by texture mapping hardware. It is not susceptible to degeneracies in the input and can be parallelized on multiprocessor systems.
5. **Efficiency:** The construction of occlusion maps takes a few milliseconds per frame on current medium- to high-end graphics systems. The culling algorithm achieves significant speedup in interactive walkthroughs of models with high depth complexity. The algorithm involves no significant preprocessing and is applicable to dynamic environments.
6. **Approximate Visibility Culling:** Our approach can also use the hierarchy of maps to perform *approximate* culling. By varying an *opacity threshold* parameter the algorithm is able to fill small transparent holes in the occlusion maps and to cull away portions of the model which are visible through small gaps in the occluders.

The resulting algorithm has been implemented on different platforms (SGI Max Impact and Infinite Reality) and applied to city models, CAD models, and dynamic environments. It obtains considerable speedup in overall frame rate. In Figure 1 we demonstrate its performance on a submarine's Auxiliary Machine Room.

**Organization:** The rest of the paper is organized as follows: . We briefly survey related work in Section 2 and give an overview of our approach in Section 3. Section 4 describes occlusion maps and techniques for fast implementation on current graphics systems. In Section 5 we describe the entire culling algorithm. We describe its implementation and performance in Section 6. Section 7 analyses our algorithm and compares it with other approaches. Finally, in Section 8, we briefly describe some future directions.

## 2 Related Work

Visibility computation and hidden surface removal are classic problems in computer graphics [FDHF90]. Some of the commonly used visibility algorithms are based on  $Z$ -buffer [Cat74] and view-frustum culling [Cla76, GBW90]. Others include Painter's Algorithm [FDHF90] and area-subdivision algorithms [War69, FDHF90].

There is significant literature on visible surface computation in computational geometry. Many asymptotically efficient algorithms have been proposed for hidden surface removal [Mul89, McK87] (see [Dor94] for a recent survey). However, the practical utility of these algorithms is unclear at the moment.

Efficient algorithms for calculating the visibility relationship among a static group of 3D polygons from arbitrary viewpoints have been proposed based on the binary space-partitioning (BSP) tree [FKN80]. The tree construction may involve considerable pre-processing in terms of time and space requirements for large models. In [Nay92], Naylor has given an output-sensitive visibility algorithm using BSPs. It uses a 2D BSP tree to represent images and presents an algorithm to project a 3D BSP tree, representing the model in object space, into a 2D BSP tree representing its image.

Many algorithms structure the model database into *cells* or regions, and use a combination of off-line and on-line algorithms for cell-to-cell visibility and the conservative computation of the potentially visible set (PVS) of primitives [ARB90, TS91, LG95]. Such approaches have been successfully used to visualize architectural models, where the division of a building into discrete rooms lends itself to a natural division of the database into cells. It is not apparent that cell-based approaches can be generalized to an arbitrary model.

Other algorithms for densely-occluded but somewhat less-structured models have been proposed by Yagel and Ray [YR96]. They used regular spatial subdivision to partition the model into cells and describe a 2D implementation. However, the resulting algorithm is very memory-intensive and does not scale well to large models.

Object space algorithms for occlusion culling in general polygonal models have been presented by Coorg and Teller [CT96b, CT96a] and Hudson et al. [Hud96]. These algorithms dynamically compute a subset of the objects as occluders and use them to cull away portions of the model. In particular, [CT96b, CT96a] compute an arrangement corresponding to a linearized portion of an aspect graph and track the viewpoint within it to check for occlusion. [Hud96] use shadow frusta and fast interference tests for occlusion culling. All of them are object-space algorithms and the choice of occluder is restricted to convex objects or simple combination of convex objects (e.g. two convex polytope sharing an edge). These algorithms are unable to combine a "forest" of small non-convex or disjoint occluders to cull away large portions of the model.

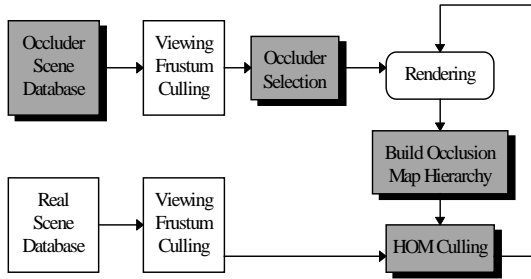
A hierarchical  $Z$ -buffer algorithm combining spatial and temporal coherence has been presented in [GKM93, GK94, Gre95]. It uses two hierarchical data structures: an octree and a  $Z$ -pyramid. The algorithm exploits coherence by performing visibility queries on the  $Z$ -pyramid and is very effective in culling large portions of high-depth complexity models. However, most current graphics systems do not support the  $Z$ -pyramid capability in hardware, and simulating it in software can be relatively expensive. In [GK94], Greene and Kass used a quadtree data structure to test visibility throughout image-space regions for anti-aliased rendering. [Geo95] describes an implementation of the  $Z$ -query operation on a parallel graphics architecture (PixelPlanes 5) for obscuration culling.

More recently, Greene [Gre96] has presented a hierarchical tiling algorithm using coverage masks. It uses an image hierarchy named a "coverage pyramid" for visibility culling. Traversing polygons from front to back, it can process densely occluded scenes efficiently and is well suited to anti-aliasing by oversampling and filtering.

For dynamic environments, Sudarsky and Gotsman [SG96] have presented an output-sensitive algorithm which minimizes the time required to update the hierarchical data structure for a dynamic object and minimize the number of dynamic objects for which the structure has to be updated.

A number of techniques for interactive walkthrough of large geometric databases have been proposed. Refer to [RB96] for a recent survey. A number of commercial systems like *Performer* [RH94], used for high performance graphics, and *Brush* [SBM<sup>+</sup>94], used for visualizing architectural and CAD models, are available. They use techniques based on view-frustum culling, levels-of-detail, etc., but have little support for occlusion culling on arbitrary models.

There is substantial literature on the visibility problem from the flight simulator community. An overview of flight simulator architectures is given in [Mue95]. Most notably, the Singer Company's Modular Digital Image Generator [Lat94] renders front to back using a hierarchy of mask buffers to skip over already cov-



**Figure 2:** *Modified graphics pipeline showing our algorithm. The shaded blocks indicate components unique to culling with hierarchical occlusion map.*

ered spans, segments or rows in the image. General Electric’s COMPU-SCENE PT2000 [Bun89] uses a similar algorithm but does not require the input polygons to be in front-to-back order and the mask buffer is not hierarchical. The Loral GT200 [LORA] first renders near objects and fills in a mask buffer, which is used to cull away far objects. Sogitec’s APOGEE system uses the Meta-Z-buffer, which is similar to hierarchical Z buffer [Chu94].

The structure of hierarchical occlusion maps is similar to some of the hierarchies that have been proposed for images, such as image pyramids [TP75], MIP maps [Wil83], Z-pyramids [GKM93], coverage pyramids [Gre96], and two-dimensional wavelet transforms like the non-standard decomposition [GBR91].

### 3 Overview

In this paper we present a novel solution to the visibility problem. The heart of the algorithm is a hierarchy of occlusion maps, which records the aggregate projection of occluders onto the image plane at different resolutions. In other words, the maps capture the cumulative occluding effects of the occluders. We use occlusion maps because they can be built quickly and have several unique properties (described later in the paper). The use of occlusion maps reflects a decomposition of the visibility problem into two sub-problems: a two-dimensional overlap test and a depth test. The former decides whether the screen space projection of the potential occludee lies completely within the screen space projection of the union of all occluders. The latter determines whether or not the potential occludee is behind the occluders. We use occlusion maps for the overlap tests, and a *depth estimation buffer* for the conservative depth test. In the conventional Z-buffer algorithm (as well as in the hierarchical Z-buffer algorithm), the overlap test is implicitly performed as a side effect of the depth comparison by initializing the Z-buffer with large numbers.

The algorithm renders the occluders at each frame and builds a hierarchy (pyramid) of occlusion maps. In addition to the model database, the algorithm maintains a separate *occluder database*, which is derived from the model database as a preprocessing step. Both databases are represented as bounding volume hierarchies. The rendering pipeline with our algorithm incorporated is illustrated in Figure 2. The shaded blocks indicate new stages introduced due to our algorithm. For each frame, the pipeline executes in two major phases:

**1. Construction of the Occlusion Map Hierarchy:** The occluders are selected from the occluder database and rendered to build the occlusion map hierarchy. This involves:

- **View-frustum culling:** The algorithm traverses the bounding volume hierarchy of the occluder database to find occluders lying in the viewing frustum.
- **Occluder selection:** The algorithm selects a subset of the occluders lying in the viewing frustum. It utilizes temporal coherence between successive frames.
- **Occluder rendering and depth estimation:** The selected occluders are rendered to form an image in the framebuffer which is the highest resolution occlusion map. Objects are rendered in pure white with no lighting or texturing. The resulting image has only black and white pixels except for antialiased edges. A depth estimation buffer is built to record the depth of the occluders.
- **Building the Hierarchical Occlusion Maps:** After occluders are rendered, the algorithm recursively filters the rendered image down by averaging blocks of pixels. This process can be accelerated by texture mapping hardware on many current graphics systems.

**2. Visibility Culling with Hierarchical Occlusion Maps:** Given an occlusion map hierarchy, the algorithm traverses the bounding volume hierarchy of the model database to perform visibility culling. The main components of this stage are:

- **View-frustum Culling:** The algorithm applies standard view-frustum culling to the model database.
- **Depth Comparison:** For each potential occludee, the algorithm conservatively checks whether it is behind the occluders.
- **Overlap test with Occlusion Maps:** The algorithm traverses the occlusion map hierarchy to conservatively decide if each potential occludee’s screen space projection falls completely within the opaque areas of the maps.

Only objects that fail one of the latter two tests (depth or overlap) are rendered.

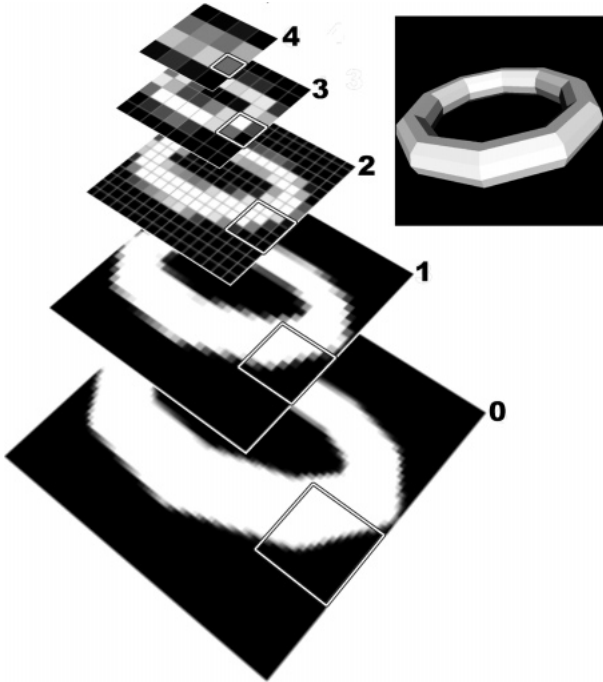
## 4 Occlusion Maps

In this section, we present occlusion maps, algorithms using texture mapping hardware for fast construction of the hierarchy of occlusion maps, and state a number of properties of occlusion maps which are used by the visibility culling algorithm.

When an opaque object is projected to the screen, the area of its projection is made opaque. The *opacity* of a block on the screen is defined as the ratio of the sum of the opaque areas in the block to the total area of the block. An *occlusion map* is a two-dimensional array in which each pixel records the opacity of a rectangular block of screen space. Any rendered image can have an accompanying occlusion map which has the same resolution and stores the opacity for each pixel. In such a case, the occlusion map is essentially the  $\alpha$  channel [FDHF90] of the rendered image (assuming  $\alpha$  values for objects are set properly during rendering), though generally speaking a pixel in the occlusion map can correspond to a block of pixels in screen space.

### 4.1 Image Pyramid

Given the lowest level occlusion map, the algorithm constructs from it a hierarchy of occlusion maps (HOM) by recursively applying the average operator to rectangular blocks of pixels. This operation forms an *image pyramid* as shown in Figure 3. The resulting hierarchy represents the occlusion map at multiple resolutions. It greatly accelerates the overlap test and is used for approximate culling. In the rest of the paper, we follow the convention that the *highest* resolution occlusion map of a hierarchy is at *level 0*.



**Figure 3:** The hierarchy of occlusion maps. This particular hierarchy is created by recursively averaging over 2 blocks of pixels. The outlined square marks the correspondence of one top-level pixel to pixels in the other levels. The image also shows the rendering of the torus to which the hierarchy corresponds.

The algorithm first renders the occluders into an image, which forms the lowest-level and highest resolution occlusion map. This image represents an *image-space fusion* of all occluders in the object space. The occlusion map hierarchy is built by recursively filtering from the highest-resolution map down to some minimal resolution (e.g.  $4 \times 4$ ). The highest resolution need not match that of the image of the model database. Using a lower image resolution for rendering occluders may lead to inaccuracy for occlusion culling near the edges of the objects, but it speeds up the time for constructing the hierarchy. Furthermore, if hardware multi-sampled anti-aliasing is available, the lowest-level occlusion map has more accuracy. This is due to the fact that the anti-aliased image in itself is already a filtered down version of a larger super-sampled image on which the occluders were rendered.

## 4.2 Fast Construction of the Hierarchy

When filtering is performed on  $2 \times 2$  blocks of pixels, hierarchy construction can be accelerated by graphics hardware that supports bilinear interpolation of texture maps. The averaging operator for  $2 \times 2$  blocks is actually a special case of *bilinear interpolation*. More precisely, the bilinear interpolation of four scalars or vectors  $\mathbf{v}_0, \mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3$  is:

$$(1 - \alpha)(1 - \beta)\mathbf{v}_0 + \alpha(1 - \beta)\mathbf{v}_1 + \alpha\beta\mathbf{v}_2 + (1 - \alpha)\beta\mathbf{v}_3,$$

where  $0 \leq \alpha \leq 1, 0 \leq \beta \leq 1$  are the weights. In our case, we use  $\alpha = \beta = 0.5$  and this formula produces the average of the four values. By carefully setting the texture coordinates, we can filter a  $2N \times 2N$  occlusion map to  $N \times N$  by drawing a two dimensional rectangle of size  $N \times N$ , texturing it with the  $2N \times 2N$  occlusion map, and reading back the rendered image as the  $N \times N$  occlusion map. Figure 4 illustrates this process.

The graphics hardware typically needs some setup time for the required operations. When the size of the map to be filtered is relatively small, setup time may dominate the computation. In such cases, the use of texture mapping hardware may slow down the computation of occlusion maps rather than accelerate it, and hierarchy building is faster on the host CPU. The break-even point between hardware and software hierarchy construction varies with different graphics systems.

[BM96] presents a technique for generating mipmaps by using a hardware accumulation buffer. We did not use this method because the accumulation buffer is less commonly supported in current graphics systems than texture mapping.

## 4.3 Properties of Occlusion Maps

The hierarchical occlusion maps for an occluder set have several desirable properties for accelerating visibility culling. The visibility culling algorithm presented in Section 5 utilizes these properties.

**1. Occluder fusion:** Occlusion maps represent the fusion of small and possibly disjoint occluders. No assumptions are made on the shape, size, or geometry of the occluders. Any object that is renderable can serve as an occluder.

**2. Hierarchical overlap test:** The hierarchy allows us to perform a fast overlap test in screen space for visibility culling. This test is described in more detail in Section 5.1.

**3. High-level opacity estimation:** The opacity values in a low-resolution occlusion map give an estimate of the opacity values in higher-resolution maps. For instance, if a pixel in a higher level map has a very low intensity value, it implies that almost all of its descendant pixels have low opacities, i.e. there is a low possibility of occlusion. This is due to the fact that occlusion maps are based on the average operator rather than the minimum or maximum operators. This property allows for a *conservative early termination* of the overlap test.

The opacity hierarchy also provides a natural method for *aggressive early termination*, or approximate occlusion culling. It may be used to cull away portions of the model visible only through small gaps in or among occluders. A high opacity value of a pixel in a low resolution map implies that most of its descendant pixels are opaque. The algorithm uses the *opacity threshold* parameter to control the degree of approximation. More details are given in Section 5.4.

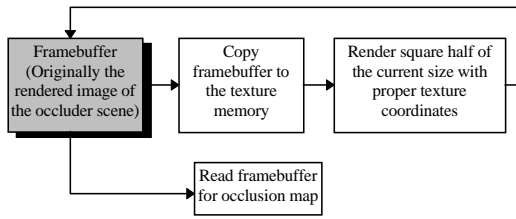
## 5 Visibility Culling with Hierarchical Occlusion Maps

An overview of the visibility culling algorithm has been presented in Section 3. In this section, we present detailed algorithms for overlap tests with occlusion maps, depth comparison, and approximate culling.

### 5.1 Overlap Test with Occlusion Maps

The two-dimensional overlap test of a potential occludee against the union of occluders is performed by checking the opacity of the pixels it overlaps in the occlusion maps. An exact overlap test would require a scan-conversion of the potential occludee to find out which pixels it touches, which is relatively expensive to do in software. Rather, we present a simple, efficient, and *conservative* solution for the overlap test.

For each object in the viewing frustum, the algorithm conservatively approximates its projection with a screen-space bounding rectangle of its bounding box. This rectangle covers a superset of the pixels covered by the actual object. The extremal values of the bounding rectangle are computed by projecting the corners



**Figure 4:** Use of texture-mapping hardware to build occlusion maps

of the bounding box. The main advantage of using the bounding rectangle is the reduced cost of finding the pixels covered by a rectangle compared to scan-converting general polygons.

The algorithm uses the occlusion map hierarchy to accelerate the overlap test. It begins the test at the level of the hierarchy where the size of a pixel in the occlusion map is approximately the same size as the bounding rectangle. The algorithm examines each pixel in this map that overlaps the bounding rectangle. If any of the overlapping pixels is not completely opaque<sup>1</sup>, the algorithm recursively descends from that pixel to the next level of the hierarchy and checks all of its sub-pixels that are covered by the bounding rectangle. If all the pixels checked are completely opaque, the algorithm concludes that the occludee’s projection is completely inside that of the occluders. If not, the algorithm conservatively concludes that the occludee may not be completely obscured by the occluders, and it is rendered.

The algorithm supports *conservative early termination* in overlap tests. If the opacity of a pixel in a low-resolution map is too low, there is small probability that we can find high opacity values even if we descend into the sub-pixels. So the overlap test stops and concludes that the object is not occluded. The *transparency thresholds* are used to define these lower bounds on opacity below which traversal of the hierarchy is terminated.

## 5.2 Depth Comparison

Occlusion maps do not contain depth information. They provide a necessary condition for occlusion in terms of overlap tests in the image plane, but do not detect whether an object is in front of or behind the occluders. The algorithm manages depth information separately to complete the visibility test. In this section, we propose two algorithms for depth comparison.

### 5.2.1 A Single Z Plane

One of the simplest ways to manage depth is to use a single Z plane. The Z plane is a plane parallel to and beyond the near plane. This plane separates the occluders from the potential occludees so that any object lying beyond the plane is farther away than any occluder. As a result, an object which is contained within the projection of the occluders and lies beyond the Z plane is completely occluded. This is an extremely simple and conservative method which gives a rather coarse bound for the depth values of all occluders.

### 5.2.2 Depth Estimation Buffer

The depth estimation buffer is a software buffer that provides a more general solution for conservatively estimating the depth of occluders. Rather than using a single plane to capture the depth

<sup>1</sup>By definition, a pixel is completely opaque if its value is above or equal to the *opacity threshold*, which is defined in Section 5.4.

of the entire set of occluders, the algorithm partitions the screen-space and uses a separate plane for each region of the partition. By using a separate depth for each region of the partition, the algorithm obtains a finer measure of the distances to the occluders. The depth estimation buffer is essentially a general-purpose software Z buffer that records the farthest distances instead of the nearest.

An alternative to using the depth estimation buffer might be to read the accurate depth values back from a hardware Z buffer after rendering the occluders. This approach was not taken mainly because it involves further assumptions of hardware features (i.e. there is a hardware Z-buffer, and we are able to read Z-values reasonably fast in a easily-usable format).

**Construction of the depth estimation buffer:** The depth estimation buffer is built at every frame, which requires determining the pixels to which the occluders project on the image plane. Scan-converting the occluders to do this would be unacceptably expensive. As we did in constructing occlusion maps, we conservatively estimate the projection and depth of an occluder by its screen-space bounding rectangle and the Z value of its bounding volume’s farthest vertex. The algorithm checks each buffer entry covered by the rectangle for possible updates. If the rectangle’s Z value is greater than the old entry, the entry is updated. This process is repeated for all occluders.

**Conservative Depth Test:** To perform the conservative depth test on a potential occludee, it is approximated by the screen space bounding rectangle of its bounding box (in the same manner as in overlap tests), which is assigned a depth value the same as that of the nearest vertex on the bounding box. Each entry of the depth estimation buffer covered by the rectangle is checked to see if any entry is greater than the rectangle’s Z value. If this is the case then the object is conservatively regarded as being partly in front of the union of all occluders and thus must be rendered.

The cost of the conservative Z-buffer test and update, though far cheaper than accurate operations, can still be expensive as the resolution of the depth estimation buffer increases. Furthermore, since we are performing a conservative estimation of the objects’ screen space extents, there is a point where increasing the resolution of the depth estimation buffer does not help increase the accuracy of depth information. Normally the algorithm uses only a coarse resolution (e.g.  $64 \times 64$ ).

## 5.3 Occluder Selection

At each frame, the algorithm selects an occluder set. The *optimal* set of occluders is exactly the visible portion of the model. Finding this optimal set is the visible surface computation problem itself. Another possibility is to pre-compute global visibility information for computing the useful occluders at every viewpoint. The fastest known algorithm for computing the effects on global visibility due to a single polyhedron with  $m$  vertices can take  $O(m^6 \log m)$  time in the worst case [GCS91].

We present algorithms to estimate a set of occluders that are used to cull a significant fraction of the model. We perform preprocessing to derive an occluder database from the model. At runtime the algorithm dynamically selects a set of occluders from that database.

### 5.3.1 Building the Occluder Database

The goal of the pre-processing step is to discard objects which do not serve as good occluders from most viewpoints. We use the following criteria to select good occluders from the model database:

- **Size:** Small objects will not serve as good occluders unless the viewer is very close to them.

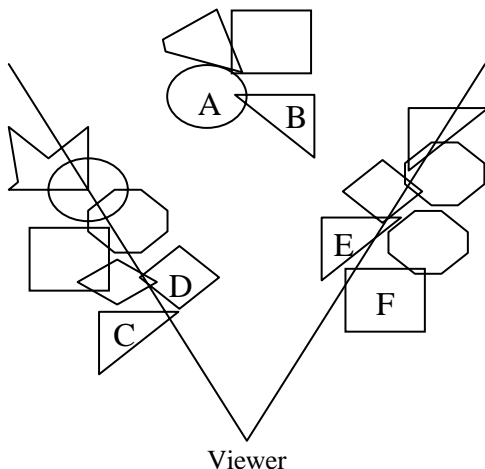


Figure 5: Distance criterion for dynamic selection

- **Redundancy:** Some objects, e.g. a clock on the wall, provide redundant occlusion and should be removed from the database.
- **Rendering Complexity:** Objects with a high polygon count or rendering complexity are not preferred, as scan-converting them may take considerable time and affect the overall frame rate.

### 5.3.2 Dynamic Selection

At runtime, the algorithm selects a set of objects from the occluder database. The algorithm uses a distance criterion, size, and temporal coherence to select occluders.

The single  $Z$ -plane method for depth comparison, presented in Section 5.2.1, is also an occluder selection method. All objects not completely beyond the  $Z$ -plane are occluders.

When the algorithm uses the depth estimation buffer, it dynamically selects occluders based on a distance criterion and a limit ( $\mathcal{L}$ ) on the number of occluder polygons. These two variables may vary between frames as a function of the overall frame rate and percentage of model culled. Given  $\mathcal{L}$ , the algorithm tries to find a set of good occluders whose total polygon count is less than  $\mathcal{L}$ .

The algorithm considers each object in the occluder database lying in the viewing frustum. The distance between the viewer and the center of an object's bounding volume is used as an estimate of the distance from the viewer to the object. The algorithm sorts these distances, and selects the nearest objects as occluder until their combined polygon count exceeds  $\mathcal{L}$ . This works well for most situations, except when a good occluder is relatively far away. One such situation has been shown in Figure 5. The distance criterion will select  $C$ ,  $D$ ,  $E$ ,  $F$ , etc. as occluders, but  $\mathcal{L}$  will probably be exceeded *before*  $A$  and  $B$  are selected. Thus, we lose occlusion that would have been contributed by  $A$  and  $B$ . In other words, there is a hole in the occlusion map which decreases the culling rate.

Dynamic occluder selection can be assisted by visibility preprocessing of the occluder scene. The model space is subdivided by a uniform grid. Visibility is sampled at each grid point by surrounding the grid point with a cube and using an item buffer algorithm similar to the hemi-cube algorithm used in radiosity. Each grid point gets a lists of visible objects. At run-time, occluders can be chosen from visible object lists of grid points nearest to the viewing point.

## 5.4 Approximate Visibility Culling

A unique feature of our algorithm is to perform approximate visibility culling, which ignores objects only visible through small holes in or among the occluders. This ability is based on an inherent property of HOM: it naturally represents the combined occluder projections at different levels of detail.

In the process of filtering maps to build the hierarchy, a pixel in a low resolution map can obtain a high opacity value even if a small number of its descendant pixels have low opacity. Intuitively, a small group of low-opacity pixels (a "hole") in a high-resolution map can dissolve as the average operation (which involves high opacity values from neighboring pixels) is recursively applied to build lower-resolution maps.

The opacity value above which the pixel is considered completely opaque is called the *opacity threshold*, which is by default 1.0. The visibility culling algorithm varies the degree of approximation by changing the opacity threshold. As the threshold is lowered, the culling algorithm becomes more approximate. This effect of the opacity threshold is based on the fact that if a pixel is considered completely opaque, the culling algorithm does not go into the descendant pixels for further opacity checking. If the opacity of a pixel in a low-resolution map is not 1.0 (because some of the pixel's descendents have low opacities), but is still higher than the opacity threshold assigned to that map, the culling algorithm does not descend to the sub-pixels to find the low opacities. In effect, some small holes in higher-resolution maps are ignored. The opacity threshold specifies the size of the holes that can be ignored; the higher the threshold, the smaller the ignorable holes.

The opacity thresholds for each level of the hierarchy are computed by first deciding the maximum allowable size of a hole. For example, if the final image is  $1024 \times 1024$  and a map is  $64 \times 64$ , then a pixel in the map corresponds to  $16 \times 16$  pixels in the final image. If we consider 25 black pixels among  $16 \times 16$  total pixels an ignorable hole, then the opacity threshold for the map is  $1 - 25/(16 * 16) = 0.90$ . Note that we are considering the worst case where the black pixels gather together to form the biggest hole, which is roughly a  $5 \times 5$  black block. One level up the map hierarchy, where resolution is  $32 \times 32$  and where a map pixel corresponds to  $32 \times 32$  screen pixels, the threshold becomes  $1 - 25/(32 * 32) = 0.98$ .

Consider the  $k$ -th level of the hierarchy. Let  $n$  black pixels among  $m$  total pixels form an ignorable hole, then the opacity threshold is  $O_k = 1 - \frac{n}{m}$ . Since at the  $k + 1$ -th level<sup>2</sup> each map pixel corresponds to four times as many pixels in the final image, the opacity threshold is

$$O_{k+1} = 1 - \frac{n}{4m} = 1 - \frac{1 - O_k}{4} = \frac{3 + O_k}{4}.$$

Let the opacity threshold in the highest resolution map be  $O_{min}$ . If a pixel in a lower resolution map has opacity lower than  $O_{min}$ , then it is not possible for all its descendant pixels have opacities greater than  $O_{min}$ . This means that if a high-level pixel is completely covered by a bounding rectangle and its opacity is lower than  $O_{min}$ , we can immediately conclude that the corresponding object is potentially visible. For pixels not completely covered by the rectangle (i.e. pixels intersecting the rectangle's edges), the algorithm always descends into sub-pixels.

To summarize the cases in the overlap test, a piece of pseudo-code is provided in 5.4.

Approximate visibility is useful because in many cases we don't expect to see many meaningful parts of the model through small holes in or among the occluders. Culling such portions of the model usually does not create noticeable visual artifacts.

<sup>2</sup>Remember that highest resolution map is level 0. See Figure 3.

```

CheckPixel(HOM, Level, Pixel, BoundingRect)
{
    Op = HOM[Level](Pixel.x, Pixel.y);
    Omin = HOM[0].OpacityThreshold;

    if (Op > HOM[Level].OpacityThreshold)
        return TRUE;
    else if (Level = 0)
        return FALSE;
    else if (Op < Omin AND
            Pixel.CompletelyInRect = TRUE)
        return FALSE;
    else
    {
        Result = TRUE;
        for each sub-pixel, Sp, that
            overlaps BoundingRect
        {
            Result = Result AND CheckPixel(HOM,
                Level-1, Sp, BoundingRect);
            if Result = FALSE
                return FALSE;
        }
    }
    return TRUE;
}

OverlapTest(HOM, Level, BoundingRect)
{
    for each pixel, P, in HOM[HOM.HighestLevel]
        that intersects BoundingRect
    {
        if (CheckPixel(HOM, HOM.HighestLevel, P)
            = FALSE)
            return FALSE;
    }
    return TRUE
}

```

**Figure 8:** Pseudo-code for the overlap test between the occlusion map hierarchy and a bounding rectangle. This code assumes that necessary information is available as fields in the *HOM* and *Pixel* structures. The meaning of the fields are easily inferred from their names. The *CheckPixel* function check the opacity of a pixel, descending into sub-pixels as necessary. The *OverlapTest* function does the whole overlap test, which returns TRUE if bounding rectangle falls within completely opaque areas and FALSE otherwise.

Omitting such holes can significantly increase the culling rate if many objects are potentially visible only through small holes. In Figure 6 and Figure 7, we illustrate approximate culling on an environment with trees as occluders.

It should be noted that in some situations approximate culling may result in noticeable artifacts, even if the opacity threshold is high. For example, if objects visible only through small holes are very bright (e.g. the sun beaming through holes among leaves of a tree), then strong popping can be observed as the viewer zooms closer. In such cases approximate culling should not be applied. Furthermore, approximate culling decreases accuracy of culling around the edges of occluders, which can also result in visual artifacts.

## 5.5 Dynamic Environments

The algorithm easily extends to dynamic environments. As no static bounding volume hierarchy may be available, the algorithm uses oriented bounding boxes around each object. The occluder selection algorithm involves no pre-processing, so the occluder

database is exactly the model database. The oriented bounding boxes are used to construct the depth estimation buffer as well as to perform the overlap test with the occlusion map hierarchy.

## 6 Implementation and Performance

We have implemented the algorithm as part of a walkthrough system, which is based on OpenGL and currently runs on SGI platforms. Significant speed-ups in frame rates have been observed on different models. In this section, we discuss several implementation issues and discuss the system's performance on SGI Max Impacts and Infinite Reality platforms.

### 6.1 Implementation

As the first step in creating the occlusion map hierarchy, occluders are rendered in a  $256 \times 256$  viewport in the back framebuffer, in full white color, with lighting and texture mapping turned off. Any one of the three color channels of the resulting image can serve as the highest-resolution occlusion map on which the hierarchy is based. An alternate method could be to render the occluders with the original color and shading parameters and use the  $\alpha$  channel of the rendered image to construct the initial map. However, for constructing occlusion maps we do not need a "realistic" rendering of the occluders, which may be more expensive. In most cases the resolution of  $256 \times 256$  is smaller than that of the final rendering of the model. As a result, it is possible to have artifacts in occlusion. In practice, if the final image is rendered at a resolution of  $1024 \times 1024$ , rendering occluders at  $256 \times 256$  is a good trade-off between accuracy and time required to filter down the image in building the hierarchy.

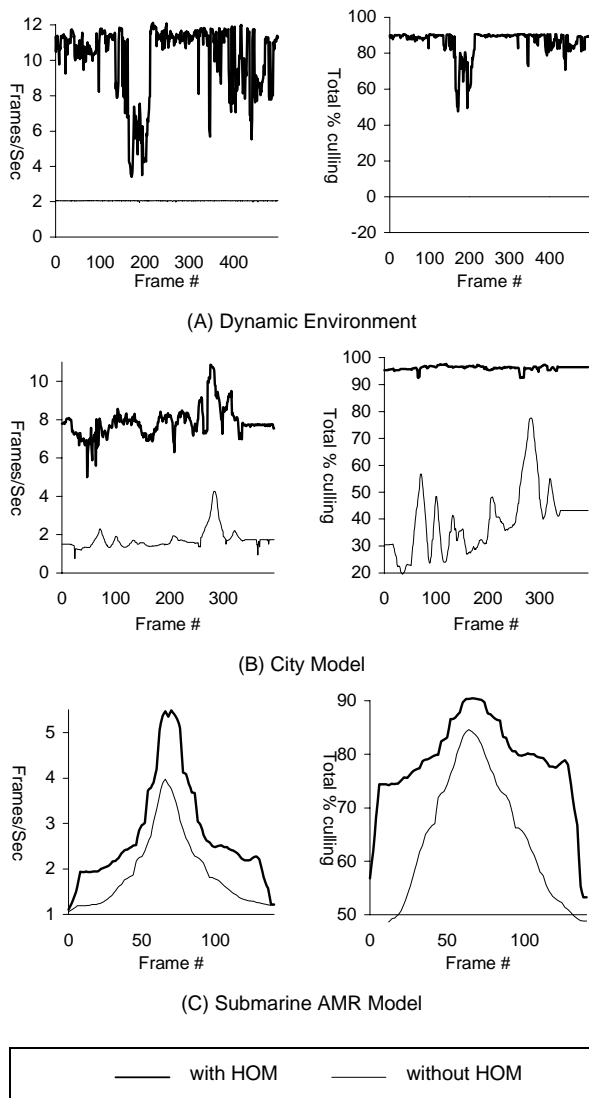
To construct the occlusion map hierarchy, we recursively average  $2 \times 2$  blocks of pixels using the texture mapping hardware as well as the host CPU. The resolution of the lowest-resolution map is typically  $4 \times 4$ . The break-even point between hardware and software hierarchy construction (as described in Section 4.2) varies with different graphics systems. For SGI Maximum Impacts, we observed the shortest construction time when the algorithm filters from  $256 \times 256$  to  $128 \times 128$  using texture-mapping hardware, and from  $128 \times 128$  to  $64 \times 64$  and finally down to  $4 \times 4$  on the host CPU. For SGI InfiniteReality, which has faster pixel transfer rates, the best performance is obtained by filtering from  $256 \times 256$  to  $64 \times 64$  using the hardware and using the host CPU thereafter. Hierarchy construction time is about 9 milliseconds for the Max Impacts and 4 milliseconds for the Infinite Reality, with a small variance (around 0.5 milliseconds) between frames.

The implementation of the depth estimation buffer is optimized for block-oriented query and updates. The hierarchical overlap test is straight-forward to implement; It is relatively harder to optimize, as it is recursive in nature.

### 6.2 Performance

We demonstrate the performance of the algorithm on three models. These are:

- **City Model:** this is composed of models of London and has 312, 524 polygons. A bird's eye view of the model has been shown in Figure 11.
- **Dynamic Environment:** It is composed of dinosaurs and teapots, each undergoing independent random motion. The total polygon count is 986, 800. It is shown in Figure 12.
- **Submarine Auxiliary Machine Room (AMR):** It is a real-world CAD model obtained from industrial sources. The



**Figure 9:** The speed-up obtained due to HOM on different models. The left graphs show the improvement in frame rate and the right graphs show the percentage of model culled. The statistics were gathered over a path for each model.

model has 632, 252 polygons. Different views of the model are shown in Figure 1 and Figure 13.

As mentioned earlier, our algorithm uses a bounding volume hierarchy (i.e. a scene graph) for both the original model database as well as the occluder database. Each model we used is originally a collection of polygons with no structure information. We construct an axis-aligned bounding box hierarchy for each database.

For the dynamic environment and the city model, we use the model database itself as the occluder database, without any pre-processing for static occluder selection. For the AMR model, the pre-processing yields an occluder database of 217, 636 polygons. The algorithm removes many objects that have little potential of being a good occluder (like the bolts on the diesel engine, thin pipes etc.) from the original model. Further, most of these parts are densely tessellated, making them to expensive to be directly used as occluders. We use the simplified version of the parts which are produced by algorithms in [Cohen96]. Although many

simplification algorithms give good error bounds on the simplified model, they do not guarantee that the projection of the simplified object lies within that of the original. Therefore, visibility artifacts may be introduced by the simplified occluders. We use very tight error bounds so that artifacts are rarely noticeable.

The performance of the algorithms has been highlighted in Figure 9. The graphs on the left show the frame rate improvement, while the graphs on the right highlight the percentage of the model culled at every frame. The performance of the city model was generated on a SGI Maximum Impact while the other two were rendered on an SGI Infinite Reality. The actual performance varies due to two reasons:

1. Different models have varying depth complexities. Furthermore, the percentage of occlusion varies with the viewpoint.
2. The ability of the occluder selection algorithm to select the "right" subset of occluders. The performance of the greedy algorithm, e.g. distance based criterion, varies with the model distribution and the viewpoint.

The occluder polygon count budget ( $\mathcal{L}$ ) per frame is important for the performance of the overall algorithm. If too few occluders are rendered, most of the pixels in the occlusion map have low opacities and the algorithm is not able to cull much. On the other hand, if too many occluder polygons are rendered, they may take a significant percentage of the total frame time and slow down the rendering algorithm. The algorithm starts with an initial guess on the polygon count and adaptively modifies it based on the percentage of the model culled and frame rate. If the percentage of the model culled is low, it increases the count. If the percentage is high and the frame rate is low, it decreases the count.

Average time spent in the different stages of the algorithm (occluder selection and rendering, hierarchy generation, occlusion culling and final rendering) has been shown in Figure 10. The average time to render the model without occlusion culling is normalized to 100%. In these cases, the average time in occluder rendering varies between 10 – 25%.

## 7 Analysis and Comparison

In this section we analyze some of the main features of our algorithm and compare it with other approaches.

Our algorithm is generally applicable to all models and obtains significant culling when there is high depth complexity. This is mainly due to its use of occlusion maps to combine occluders in image space. The extensive use of screen space bounding rectangles as an approximation of the object's screen space projection makes the overlap tests and depth tests fast and cheap.

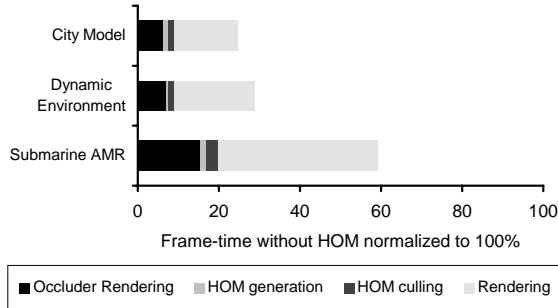
In terms of hardware assumptions, the algorithm requires only the ability to read back the framebuffer. Texture mapping with bilinear interpolation, when available, can be directly used to accelerate the construction of the occlusion map hierarchy.

In general, if the algorithm is spending a certain percentage of the total frame time in occluder rendering, HOM generation and culling (depth test and overlap test), it should at least cull away a similar percentage of the model so as to justify the overhead of occlusion culling. If a model under some the viewing conditions does *not* have sufficient occlusion, the overall frame rate may decrease due to the overhead, in which case occlusion culling should be turned off.

### 7.1 Comparison to Object Space Algorithms

Work on cells and portals[ARB90, TS91, LG95] addresses a special class of densely occluded environments where there are plenty





**Figure 10:** Average speed-up obtained due to HOM culling on different models. The total time to render each model without HOM culling is normalized to 100%. Each bar shows the percentage of time spent in different stages of our algorithm.

of cell and portal structures, as in an indoor architectural model. [ARB90, TS91] pre-processes the model to identify potentially visible set of primitives for each cell. [LG95] developed a dynamic version which eliminates the visibility pre-processing. These methods work very well for this particular type of environment, but are not applicable to models without cell/portal structures.

Our algorithm works without modification for environments with cells and portals, but occluder selection can be optimized for these environments. The cell boundaries can be used to form the occluder database. As an alternative, we can fill a viewport with white pixels and then render the portals in black to form the occlusion map. In general, however, we do not expect to outperform the specialized algorithms in cell/portal environments.

Two different object space solutions for more general models have been proposed by [CT96a, CT96b] and [Hud96]. They dynamically choose polygons and convex objects (or simple convex combination of polygons) as occluders and use them to cull away invisible portions of the model. However, many models do not have single big convex occluders. In such cases, merging small, irregular occluders is critical for significant culling, which is a difficult task in object space. Our algorithm lies between object space and image space and the occluder merging problem is solved in image space.

## 7.2 Comparison with Hierarchical Z-buffer Algorithm

In many ways, we present an alternative approach to hierarchical Z-buffer visibility [GKM93]. The main algorithm presented in [GKM93] performs updates of the Z-buffer hierarchy as geometry is rendered. It assumes special-purpose hardware for fast depth updating and querying to obtain interactive performance. It is potentially a very powerful and effective algorithm for visibility culling. However, we are not aware of any hardware implementation.

There is a possible variation of hierarchical Z-buffer algorithm which selects occluders, renders them, reads back the depth buffer once per frame, builds the Z-pyramid, and use the screen-space bounding rectangles for fast culling. The algorithm proposed in [GKM93] uses the exact projection of octree nodes, which requires software scan-conversion. In this case, the HOM approach and the hierarchical Z-buffer are comparable, each with some advantages over the other.

The HOM approach has the following advantages:

1. There is no need for a Z-buffer. Many low-end systems do

not support a Z-buffer and some image generators for flight simulators do not have one. Tile-based architectures like PixelFlow[MEP92] and Talisman[TK96] do not have a full-screen Z-buffer, but instead have volatile Z-buffers the size of a single tile. This makes getting Z values for the entire screen rather difficult.

2. The construction of HOM has readily-available hardware support (in the form of texture mapping with bilinear interpolation) on many graphics systems. Further, if filtering is performed in software, the cost of the average operator is smaller than the minimum/maximum operator (due to the absence of branch instructions).
3. HOM supports conservative early termination in the hierarchical test by using a transparency threshold (Section 5.1) and approximate occlusion culling by using an opacity threshold (Section 5.4). These features result from using an average operator.

On the other hand, the Hierarchical Z-buffer has depth values, which the HOM algorithm has to manage separately in the depth estimation buffer. This results in the following advantages of Hierarchical Z-buffer:

1. Culling is less conservative.
2. It is easier to use temporal coherence for occluder selection because nearest Z values for objects are available in the Z-buffer. Updating the active occluder list is more difficult in our algorithm since we only have estimated farthest Z values.

## 7.3 Comparison with Hierarchical Tiling with Coverage Masks

Hierarchical polygon tiling [Gre96] tiles polygons in front-to-back order and uses a “coverage” pyramid for visibility culling. The coverage pyramid and hierarchical occlusion maps serve the same purpose in that they both record the aggregate projections of objects. (In this sense, our method has more resemblance to hierarchical tiling than to the hierarchical Z-buffer.) However, a pixel in a mask in the coverage pyramid has only three values (covered, vacant or active), while a pixel in an occlusion map has a continuous opacity value. This has lead to desirable features, as discussed above. Like HOM, the coverage masks do not contain depth information and the algorithm in [Gre96] uses a BSP-tree for depth-ordering of polygons. Our algorithm is not restricted to rendering the polygons front to back. Rather, it only needs a conservatively estimated boundary between the occluders and potential occludees, which is represented by the depth estimation buffer. Hierarchical tiling is tightly coupled with polygon scan-conversion and has to be significantly modified to deal with non-polygonal objects, such as curved surfaces or textured billboards. Our algorithm does not directly deal with low-level rendering but utilizes existing graphics systems. Thus it is readily applicable to different types of objects so long as the graphics system can render them. Hierarchical tiling requires special-purpose hardware for real-time performance.

## 8 Future Work and Conclusion

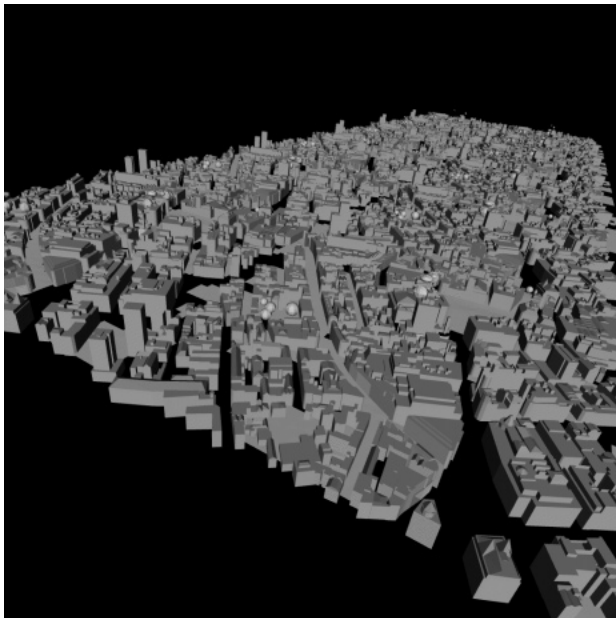
In this paper we have presented a visibility culling algorithm for general models that achieves significant speedups for interactive walkthroughs on current graphics systems. It is based on hierarchical occlusion maps, which represent an image space fusion of all the occluders. The overall algorithm is relatively simple, robust and easy to implement. We have demonstrated its performance on a number of large models.

There are still several areas to be explored in this research. We believe the most important of these to be occlusion preserving simplification algorithms, integration with levels-of-detail modeling, and parallelization.

**Occlusion Preserving Simplification:** Many models are densely tessellated. For fast generation of occlusion maps, we do not want to spend considerable time in rendering the occluders. As a result, we are interested in simplifying objects under the constraint of occlusion preservation. This implies that the screen space projection of the simplified object should be a subset of that of the original object. Current polygon simplification algorithms can reduce the polygon count while giving tight error bounds, but none of them guarantees an occlusion preserving simplification.

**Integration with Level-of-Detail Modeling:** To display large models at interactive frame rates, our visibility culling algorithm needs to be integrated with level-of-detail modeling. The latter involves polygon simplification, texture-based simplification and dynamic tessellation of higher order primitives.

**Parallelization:** Our algorithm can be easily parallelized on multi-processor machines. Different processors can be used for view frustum culling, overlap tests and depth tests.

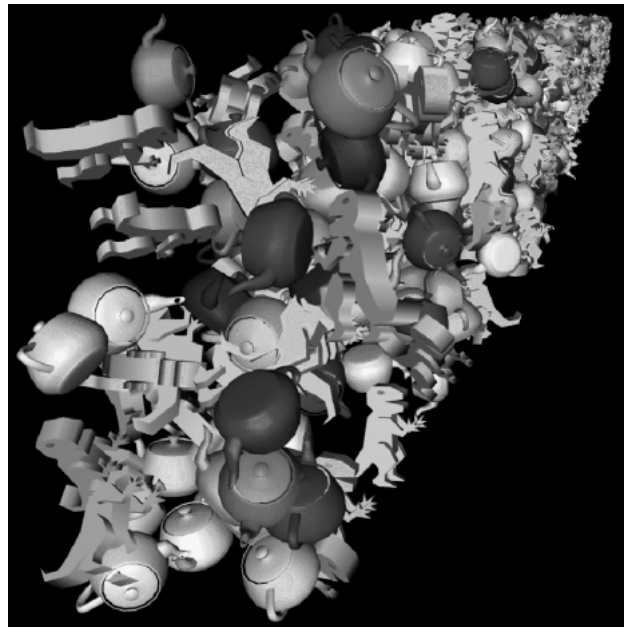


**Figure 11:** City model with 312,524 polygons. Average speed-up obtained by our visibility culling algorithm is about five times.

## 9 Acknowledgements

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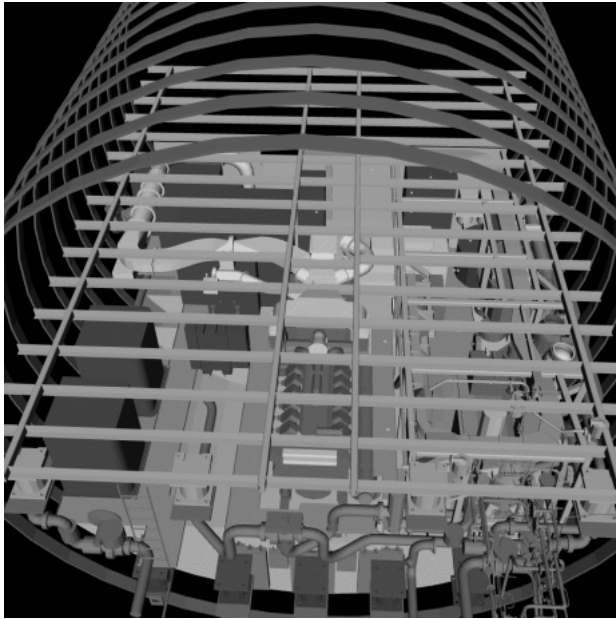


**Figure 12:** Dynamic environment composed of dinosaurs and teapots. The total polygon count is 986,800. The HOM algorithm achieves about five times speed-up.

the NSF/ARPA Center for Computer Graphics and Scientific Visualization, and a UNC Board of Governors Fellowship.

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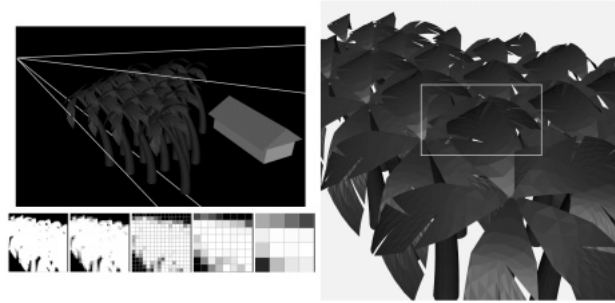
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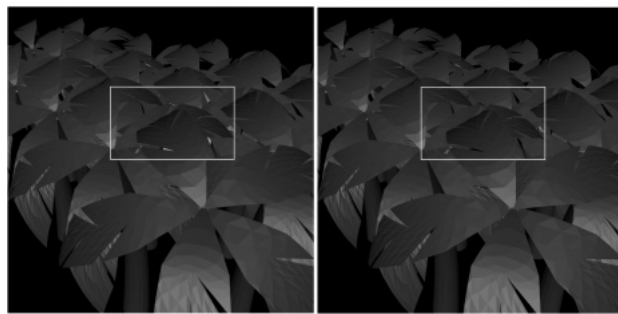
**Figure 13:** A top view of the auxiliary machine room of a submarine composed of 632,252 polygons. Average speed-up is about two due to occlusion culling.

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**Figure 6:** *These images show a view of an environment composed of trees and a house, with the trees as occluders. The green line in the left image indicates the view-frustum. The right image highlights the holes among the leaves with a yellow background. The screen space bounding rectangle of the house is shown in cyan. The occlusion map hierarchy is shown on the left.*



**Figure 7:** *Two images from the same view as in Figure 6. The left image is produced with no approximate culling. The right image uses opacity threshold values from 0.7 for the highest resolution map up to 1.0 for the lowest resolution map.*